



1. A random sample of 35 homeowners was taken from each of the villages Greenslax and Penville and their ages were recorded. The results are summarised in the back-to-back stem and leaf diagram below.

Totals	Greenslax						Penville					Totals							
(2)			8	7	2		5	5	6	7	8	8	9	(7)					
(3)			9	8	7		3	1	1	1	2	3	4	4	5	6	7	9	(11)
(4)			4	4	4	0		4	0	1	2	4	7	(5)					
(5)			6	6	5	2	2		5	0	0	5	5	5	(5)				
(7)	8	6	5	4	2	1	1		6	2	5	6	6	(4)					
(8)	8	6	6	6	4	3	1	1		7	0	5	(2)						
(5)			9	8	4	3	2		8									(0)	
(1)					4		9	9										(1)	

Key: 7 | 3 | 1 means 37 years for Greenslax and 31 years for Penville

Some of the quartiles for these two distributions are given in the table below.

	Greenslax	Penville
Lower quartile, $Q_1$	$a$	31
Median, $Q_2$	64	39
Upper quartile, $Q_3$	$b$	55

- (a) Find the value of  $a$  and the value of  $b$ . (2)

An outlier is a value that falls either

more than  $1.5 \times (Q_3 - Q_1)$  above  $Q_3$

or more than  $1.5 \times (Q_3 - Q_1)$  below  $Q_1$

- (b) On the graph paper opposite draw a box plot to represent the data from Penville. Show clearly any outliers. (4)

- (c) State the skewness of each distribution. Justify your answers. (3)

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5. The discrete random variable  $X$  has the probability function

$$P(X = x) = \begin{cases} kx & x = 2, 4, 6 \\ k(x - 2) & x = 8 \\ 0 & \text{otherwise} \end{cases}$$

where  $k$  is a constant.

(a) Show that  $k = \frac{1}{18}$  **(2)**

(b) Find the exact value of  $F(5)$ . **(1)**

(c) Find the exact value of  $E(X)$ . **(2)**

(d) Find the exact value of  $E(X^2)$ . **(2)**

(e) Calculate  $\text{Var}(3 - 4X)$  giving your answer to 3 significant figures. **(3)**

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6. The times, in seconds, spent in a queue at a supermarket by 85 randomly selected customers, are summarised in the table below.

Time (seconds)	Number of customers, $f$
0 – 30	2
30 – 60	10
60 – 70	17
70 – 80	25
80 – 100	25
100 – 150	6

A histogram was drawn to represent these data. The 30 – 60 group was represented by a bar of width 1.5 cm and height 1 cm.

- (a) Find the width and the height of the 70 – 80 group. (3)

- (b) Use linear interpolation to estimate the median of this distribution. (2)

Given that  $x$  denotes the midpoint of each group in the table and

$$\sum fx = 6460 \quad \sum fx^2 = 529\,400$$

- (c) calculate an estimate for
- (i) the mean,
  - (ii) the standard deviation,
- for the above data. (3)

One measure of skewness is given by

$$\text{coefficient of skewness} = \frac{3(\text{mean} - \text{median})}{\text{standard deviation}}$$

- (d) Evaluate this coefficient and comment on the skewness of these data. (3)

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