



1. Given  $y = x^3 + 4x + 1$ , find the value of  $\frac{dy}{dx}$  when  $x = 3$

(4)

Q1

(Total 4 marks)



2. Express  $\frac{15}{\sqrt{3}} - \sqrt{27}$  in the form  $k\sqrt{3}$ , where  $k$  is an integer. (4)

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(Total 4 marks)

Q2







4. The line  $L_1$  has equation  $4x + 2y - 3 = 0$

(a) Find the gradient of  $L_1$ .

(2)

The line  $L_2$  is perpendicular to  $L_1$  and passes through the point (2, 5).

(b) Find the equation of  $L_2$  in the form  $y = mx + c$ , where  $m$  and  $c$  are constants.

(3)

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6. A sequence  $x_1, x_2, x_3, \dots$  is defined by

$$x_1 = 1$$

$$x_{n+1} = (x_n)^2 - kx_n, \quad n \geq 1$$

where  $k$  is a constant,  $k \neq 0$

(a) Find an expression for  $x_2$  in terms of  $k$ . (1)

(b) Show that  $x_3 = 1 - 3k + 2k^2$  (2)

Given also that  $x_3 = 1$ ,

(c) calculate the value of  $k$ . (3)

(d) Hence find the value of  $\sum_{n=1}^{100} x_n$  (3)

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7. Each year, Abbie pays into a savings scheme. In the first year she pays in £500. Her payments then increase by £200 each year so that she pays £700 in the second year, £900 in the third year and so on.

- (a) Find out how much Abbie pays into the savings scheme in the tenth year. (2)

Abbie pays into the scheme for  $n$  years until she has paid in a total of £67200.

- (b) Show that  $n^2 + 4n - 24 \times 28 = 0$  (5)

- (c) Hence find the number of years that Abbie pays into the savings scheme. (2)

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8. A rectangular room has a width of  $x$  m.

The length of the room is 4 m longer than its width.

Given that the perimeter of the room is greater than 19.2 m,

(a) show that  $x > 2.8$  (3)

Given also that the area of the room is less than 21 m<sup>2</sup>,

(b) (i) write down an inequality, in terms of  $x$ , for the area of the room.  
 (ii) Solve this inequality. (4)

(c) Hence find the range of possible values for  $x$ . (1)

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9.

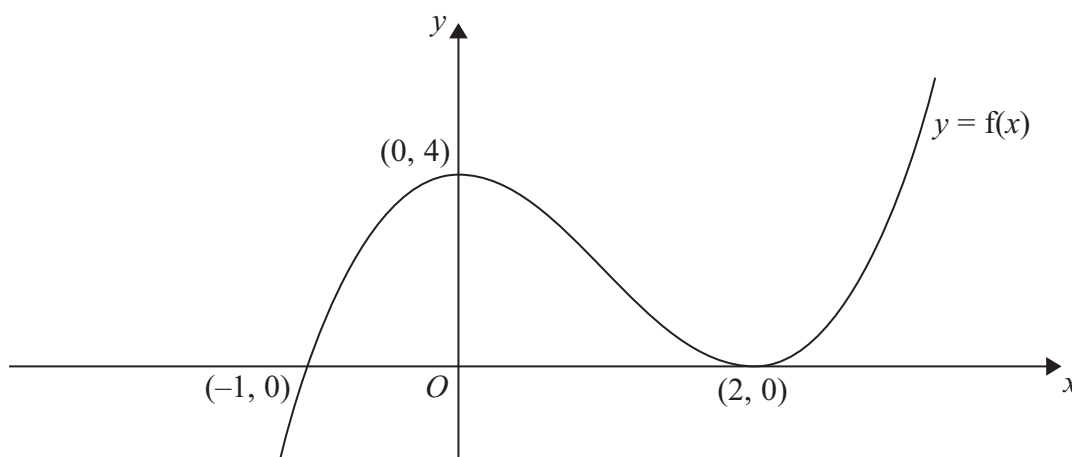


Figure 1

Figure 1 shows a sketch of the curve  $C$  with equation  $y = f(x)$ .

The curve  $C$  passes through the point  $(-1, 0)$  and touches the  $x$ -axis at the point  $(2, 0)$ .

The curve  $C$  has a maximum at the point  $(0, 4)$ .

(a) The equation of the curve  $C$  can be written in the form

$$y = x^3 + ax^2 + bx + c$$

where  $a$ ,  $b$  and  $c$  are integers.

Calculate the values of  $a$ ,  $b$  and  $c$ .

(5)

(b) Sketch the curve with equation  $y = f(\frac{1}{2}x)$  in the space provided on page 24

Show clearly the coordinates of all the points where the curve crosses or meets the coordinate axes.

(3)

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**Question 9 continued**





**Question 9 continued**

Lined area for writing the answer to Question 9.

**(Total 8 marks)**

**Q9**











11.

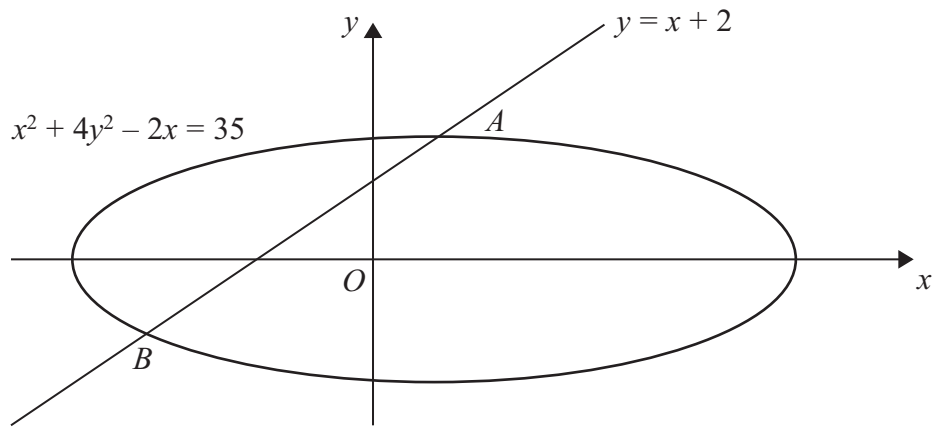


Figure 2

The line  $y = x + 2$  meets the curve  $x^2 + 4y^2 - 2x = 35$  at the points  $A$  and  $B$  as shown in Figure 2.

- (a) Find the coordinates of  $A$  and the coordinates of  $B$ . (6)
- (b) Find the distance  $AB$  in the form  $r\sqrt{2}$  where  $r$  is a rational number. (3)

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